



## Properties and atomic structure of amorphous early transition metals

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### ABSTRACT

Recently, we studied the properties of amorphous Zr–TL alloys (TL = Ni, Cu) in order to obtain parameters associated with the electronic structure and interatomic bonding of amorphous Zr. Here, we provide new data for the magnetic, superconducting and mechanical properties of amorphous Hf–TL and Ti–TL alloys. We combine our results with published data in order to obtain parameters appropriate to hypothetical amorphous Hf and Ti. These parameters are very different from those of the stable crystalline phases (hcp) of Hf and Ti and indicate, as for Zr, an fcc-like short range order for amorphous Hf and Ti. This results in an enhanced electronic density of states at the Fermi level, but in weakened interatomic bonding.

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## 1. Introduction

Amorphous TE–TL alloys (TE = Ti, Zr, Hf and TL = Ni, Cu) have been extensively studied in recent decades and interest in these alloys further increased following the discovery of TE–TL based bulk metallic glasses (BMGs) [1]. TE–TL alloys show wide glass-forming ranges which enables detailed study of the change in the electronic structure and properties on alloying and, thus a thorough comparison between the model and experimental data [2].

In amorphous TE–TL alloys the properties that are directly related to the electronic density of states (DOS) often show linear variations with TL content [2–5]. This finding correlates with ultraviolet photoemission spectroscopy (UPS) results [6] which show that, in these alloys, the DOS at the Fermi level ( $E_F$ ),  $N(E_F)$ , is dominated by TE d-states and is reduced on increasing the TL content. Therefore, the effect of alloying with TL can be approximated by the dilution of amorphous TE [3,5]. Thus, one can extrapolate the data for glassy TE–TL alloys to zero TL content in order to deduce the properties of amorphous (a) TE. This method has been used to obtain the  $N(E_F)$  and probable local atomic structure of a-Ti and a-Zr [2]. More recently, the same approach has been used to obtain the atomic volumes of a-TE [4] and the magnetic, superconducting and mechanical properties of a-Zr [5,7]. The derived parameters for a-Ti,

Zr agree quite well with those calculated for cubic phases of these metals [8] and are quite different from those of the stable crystalline phases (hcp) of TEs. This result is plausible since the amorphous atomic arrangement is incompatible with the anisotropy of the hcp lattice.

The majority of the results for TE–TL metallic glasses have been obtained for Zr–TL alloys, so that a comparison between the alloy systems based on different TE is seldom possible [2,4,9]. Here, we report new results for the magnetic, superconducting and mechanical properties of several Ti–Cu and Hf–Cu glassy alloys and combine these results with the literature data for Ti–TL and Hf–TL metallic glasses in order to observe how a change in TE (Ti → Zr → Hf) affects these properties for glassy TE–TL alloys. We also estimate some parameters of hypothetical pure a-TE and compare them with those for crystalline phases of TE.

## 2. Experimental

The  $Hf_{100-x}Cu_x$  ( $30 \leq x \leq 70$ ) and  $Ti_{100-x}Cu_x$  ( $35 \leq x \leq 55$ ) glassy alloys were prepared in the form of thin ribbons by melt spinning of arc-melted alloys in a controlled He atmosphere. Casting with controlled parameters resulted in ribbons with closely similar cross-sections ( $\sim 2 \text{ mm} \times 0.03 \text{ mm}$ ) and, thus, with the glassy phase having broadly the same degree of quenched-in disorder. As-cast samples were used for actual measurements and their fully amorphous structures were verified by X-ray diffraction [9]. The superconducting transition temperatures  $T_c$  were determined either resistively, or via ac susceptibility measurements [3,9]. The magnetic susceptibility was measured with a SQUID magnetometer MPMS [10] in a magnetic field  $B \leq 5.5 \text{ T}$  over the temperature range of 5–300 K. The Young's modulus,  $E$ , was calculated from the relationship  $E = \rho v_E^2$ , where  $\rho$  is the density of the alloy and  $v_E$  the velocity of ultrasonic waves along the ribbon.  $v_E$  was measured with a pulse-echo

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**Table 1**

The parameters of amorphous Ti, Zr and Hf compared with those for different crystalline phases of the same metals. The values for  $N(E_F)$ ,  $\chi_{\text{exp}}$  and  $\chi_p$  of  $\alpha(\text{hcp})$  and fcc phase (calculated) are taken from [8].

	Structure	$N(E_F)$ (states/eV atom)	$\chi_{\text{exp}}$ ( $\times 10^3 \text{ JT}^{-2} \text{ mol}^{-1}$ )	$\chi_p$ ( $\times 10^3 \text{ JT}^{-2} \text{ mol}^{-1}$ )	$T_c$ (K)	$E$ (GPa)
Ti	Amorphous	2.0	2.11	1.2	2.0	80
	$\alpha(\text{hcp})$	1.03	1.40	0.44	0.4	116
	fcc	1.76	2	1.22		
Zr	Amorphous	1.55	1.58	0.84	5.5	40
	$\alpha(\text{hcp})$	0.84	1.08	0.42	0.8	68
	fcc	1.34	1.50	0.69		
Hf	Amorphous		1.2	0.7	3.5	60
	$\alpha(\text{hcp})$	0.68	0.71	0.29	0.1	78
	fcc	1.45	1.1	0.79		

technique at room temperature [7]. The density,  $\rho$ , of the samples was measured by the Archimedes method [3]. The estimated error was around  $\pm 2\%$ .

The experimental procedures used to obtain published data can be found in the original papers. The (extrapolated) values for some properties of pure amorphous Ti, Zr and Hf are compared with those of the respective crystalline phases of these metals in Table 1.

### 3. Results and discussion

As pointed out in Section 1, the band structure of amorphous TE–TL alloys results in DOS with d-states for TE at  $E_F$  and those for TL well below  $E_F$  [2,6]. Such a DOS results in an approximately linear decrease of  $N(E_F)$  with increasing TL content  $x$ , for  $x \leq 65$  [2]. In Zr–TL and Ti–TL alloys [2] the values of  $N(E_F)$  were obtained from the measurements of low temperature specific heat (LTSH) and superconducting transition temperature,  $T_c$ . LTSH yields the Debye temperature,  $\theta_D$ , and dressed DOS at  $E_F$ ,  $N_\gamma(E_F) = (1 + \lambda_{\text{ep}})N(E_F)$  (with  $\lambda_{\text{ep}}$  the electron–phonon enhancement), while  $T_c$  enables [2] the calculation of  $\lambda_{\text{ep}}$ .  $N_\gamma(E_F)$  can also be calculated from the normal state resistivity  $r$ , density  $\rho$ , and the temperature dependence of the upper critical field,  $H_{c2}(T)$  [9]:

$$N_\gamma(E_F) = \frac{-\pi M}{4k_B N_A \rho r} \left( \frac{dH_{c2}}{dt} \right)_{t=1}, \quad (1)$$

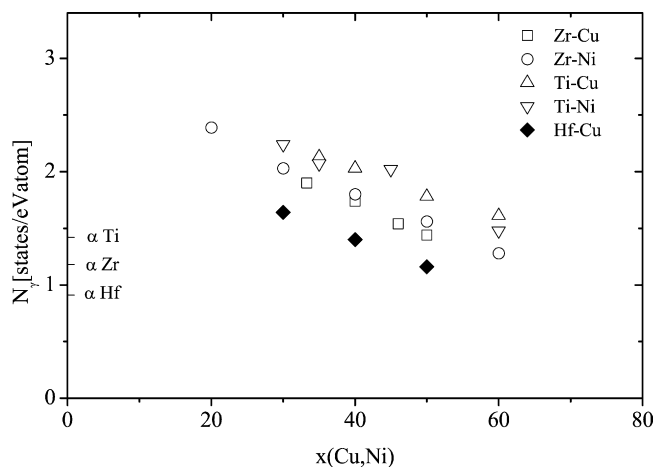
where  $k_B$  is the Boltzmann constant,  $N_A$  the Avogadro's number,  $M$  the molecular weight and  $t = T/T_c$ . We applied this method to Hf–Cu alloys for which there are no LTSH results. As shown in Fig. 1,  $N_\gamma(E_F)$  for all TE–TL glassy alloys decreases linearly with TL content ( $x$ ). Since  $\lambda_{\text{ep}}$  also decreases approximately linearly [2] with  $x$ , the corresponding variation of  $N(E_F)$  in TE–TL alloys should be qualitatively the same as that of  $N_\gamma(E_F)$ . The  $N_\gamma(E_F)$  values in Fig. 1 decrease in the sequence Ti  $\rightarrow$  Zr  $\rightarrow$  Hf, which is mainly due to increasing band-

width in the same sequence [8]. At low TL contents,  $N_\gamma(E_F)$  values for all the TE–TL glassy alloys are substantially larger than those of corresponding pure crystalline (hcp) TEs (Fig. 1). The enhanced  $N_\gamma(E_F)$  and  $N(E_F)$  in a-TEs is probably due to absence of a local minimum in the DOS at  $E_F$  which occurs in hcp phases of crystalline TE and is absent in cubic phases of the same metals [8]. Indeed, the values of  $N(E_F)$  for a-Ti [2] and a-Zr [5] are close to those calculated for fcc phases of these metals [8] (Table 1). The absence of any hcp atomic arrangements in a-TEs and their alloys has a profound influence on their DOS and interatomic bonding and, hence, affects all properties of glassy TE–TL alloys.

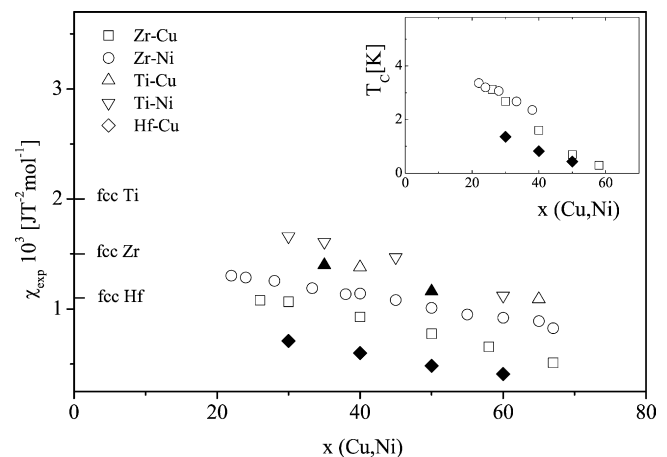
Quite large  $N(E_F)$  and its simple variation with  $x$  strongly affect the magnetic and superconducting properties of glassy TE–TL alloys [5,9]. As shown in Fig. 2, in paramagnetic alloys with TL=Ni, Cu magnetic susceptibility,  $\chi_{\text{exp}}$ , decreases approximately linearly with  $x$  and for the same  $x$   $\chi_{\text{exp}}$  decreases in the sequence Ti  $\rightarrow$  Zr  $\rightarrow$  Hf. Also, the extrapolations of  $\chi_{\text{exp}}$  plots in Fig. 2 to  $x=0$  ( $0=\text{TE}$ ) yield values which are considerably larger than those for hcp TE, but agree quite well with those calculated [8] for fcc phases of these metals (Table 1). In spite of the apparent similarity between  $N(E_F)$  vs.  $x$  [2] and  $\chi_{\text{exp}}$  vs.  $x$  (Fig. 2) plots, the description of  $\chi_{\text{exp}}$  for transition metals is somewhat more involved:

$$\chi_{\text{exp}} = \chi_p + \chi_{\text{ion}} + \chi_{\text{orb}}, \quad (2)$$

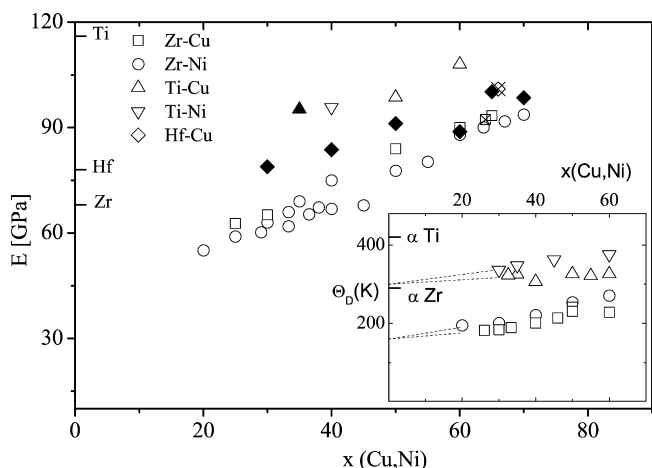
where  $\chi_{\text{ion}}$  and  $\chi_{\text{orb}}$  are, respectively, the temperature-independent ionic core diamagnetism and the orbital paramagnetism. The Pauli paramagnetism of the d-band,  $\chi_p$ , is enhanced over the free-electron value,  $\chi_p^0$ , due to exchange interaction.  $\chi_p = S\chi_p^0$ , where  $S$  is the Stoner enhancement factor [5,15] and, in TE,  $\chi_p$  is only weakly dependent on temperature [8].



**Fig. 1.** Dressed densities of states  $N_\gamma(E_F)$  of Zr–Cu [11], Zr–Ni [12], Ti–Cu [13], Ti–Ni [14] and Hf–Cu alloys vs. Cu, Ni content  $x$ . Full symbols denote present data.



**Fig. 2.** Magnetic susceptibility  $\chi_{\text{exp}}$  of Zr–Cu [3], Zr–Ni [3,15], Ti–Cu [13], Ti–Ni [14], and Hf–Cu alloys vs. Cu, Ni content  $x$ . Susceptibilities of pure fcc Ti, Zr and Hf [8] are shown for comparison. (Inset) Superconducting transition temperatures  $T_c$  of Zr–Cu [3], Zr–Ni [3] and Hf–Cu alloys vs. Ni, Cu content  $x$ . Full symbols denote present data.



**Fig. 3.** Young's modulus  $E$  for Zr–Cu [16,17], Zr–Ni [16,18], Ti–Cu [19], Ti–Ni [17], Hf<sub>34</sub>Cu<sub>66</sub> [20], Zr<sub>36</sub>Cu<sub>64</sub> [21], Hf–Cu and Ti<sub>65</sub>Cu<sub>35</sub> alloys vs. Cu,Ni content  $x$  (crossed symbols are bulk alloys).  $E$  of pure ( $\alpha$ ) Ti, Zr and Hf are also shown. (Inset) Debye temperatures  $\theta_D$  of Zr–Cu [11,22], Zr–Ni [12], Ti–Cu [13] and Ti–Ni [14] alloys vs. Cu,Ni content  $x$ .  $\theta_D$  for pure ( $\alpha$ ) Ti and Zr are also shown. Full symbols denote present data.

The expression (1) can also be applied to glassy TE–TL alloys, with  $\chi_{ion}$  and  $\chi_{orb}$  of the constituents scaled to their atomic fractions in the alloy [5], which enables one to extract  $\chi_p$  from  $\chi_{exp}$ . For TE = Ti, Zr, Hf, the bandwidth increases in the sequence Ti  $\rightarrow$  Zr  $\rightarrow$  Hf which leads to a decrease of both  $\chi_p$  (via the decrease of the bare DOS at  $E_F$ ,  $N(E_F)$ , in  $\chi_p^0$ ) and  $\chi_{orb}$  [8], in the same order. The lack of reliable  $N(E_F)$  data for Hf-based alloys [2,9] prevents a detailed analysis of their  $\chi_{exp}$  in terms of Eq. (1). The values of  $\chi_p$  for all a-TEs agree well with those calculated for fcc phases of corresponding TEs [8] and are substantially larger than those of their  $\alpha$ -phases (hcp) (Table 1). In particular,  $\chi_p$  for a-Zr is double that for  $\alpha$ -Zr.

The enhanced  $N(E_F)$  for a-TEs is also the main reason that the  $T_c$ 's for Zr and Hf-based glassy alloys are well above those for pure crystalline Zr and Hf (inset to Fig. 2). The approximately linear variations of  $T_c$  with  $x$  in these alloys extrapolate to  $T_c$ 's of amorphous Zr and Hf which are about an order of magnitude higher than those of crystalline Zr and Hf (Table 1). The larger ionic mass of Hf than that of Zr contributes to lower  $T_c$ 's of Hf-based alloys. Surprisingly, glassy Ti-based alloys having the highest  $N(E_F)$  show the lowest  $T_c$ 's, which implies very inefficient electron–phonon coupling in these alloys [9].

In Fig. 3 we show the variations of the Young's modulus,  $E$ , in TE–TL glassy alloys with TL content  $x$ . Comparing Fig. 3 with Fig. 1, we note that, in all these alloy systems, a linear decrease of  $N_\gamma(E_F)$  (also  $N(E_F)$ ) is accompanied by an approximately linear increase of  $E$  with  $x$ . Thus, a simple relationship between DOS at  $E_F$  and the elastic stiffness ( $E$ ), first observed in Zr–TL metallic glasses [7], seems to hold also for other TE–TL glassy alloys. In binary amorphous metal–metal alloys such as the TE–TL glassy alloys the dense random packing of constituent atoms [2,4] suggests a direct link between their Young's modulus and the strength of the interatomic bonding [7,24]. Thus, an approximately linear increase of  $E$  with  $x$  implies an increase in the strength of bonding, which correlates with the simultaneous decrease of the DOS at  $E_F$  ( $N_\gamma(E_F)$ ,  $N(E_F)$ ) with  $x$  (Fig. 1). Accordingly, the enhanced DOS at  $E_F$  in a-TE is associated with a Young's modulus which is substantially smaller than that of the corresponding crystalline (hcp) TE (Fig. 3 and Table 1). We note that the values of  $E$  for binary BMG alloys in the Zr–Cu and Hf–Cu systems fall well within the ranges of the data for other compositions from the same alloy systems (Fig. 3).

Since the amorphous alloys are approximately isostructural [23], their vibrational spectra should be quite similar [24], thus

their Debye temperatures,  $\theta_D$ , should also be directly related to the strength of interatomic bonding. Indeed, as illustrated in the inset to Fig. 3, the variations of  $\theta_D$  for Zr–TL and Ti–TL glassy alloys with TL content are qualitatively similar to those of  $E$  with  $x$  (Fig. 3) for alloys in these systems. The extrapolated values of  $\theta_D$  for a-Zr and a-Ti are much lower than those of crystalline Zr and Ti (Fig. 3), which is consistent with weak interatomic bonding in a-TEs.

Since the amorphous alloys are macroscopically homogenous and isotropic systems, their elastic moduli are correlated. Thus, the shear modulus,  $G$ , and the bulk modulus,  $B$ , can be calculated from the known  $E$  and the Poisson's ratio  $\sigma$  [5,7]. Furthermore, the absence of extended crystal defects [23] in metallic glasses leads to very large hardness,  $H_v$ , and also to a direct relationship between  $H_v$  and the strength of the interatomic bonding [7]. Thus, the  $H_v$  for TE–TL glasses should be proportional to the elastic moduli [7,17] and, therefore, should increase with TL content within the explored concentration range. This was verified for Zr–TL alloys [7]; measurements of  $H_v$  for Hf–Cu and Ti–TL alloys are in progress.

#### 4. Conclusion

New results for the properties of Ti–TL and Hf–TL alloys are presented and have been combined with literature data in order to obtain an insight into the electronic structure/property relationships for all the TE–TL metallic glasses and to predict, by extrapolation, the properties of pure amorphous TE (Table 1). Density of states,  $N(E_F)$  for TE-rich glassy alloys is considerably larger than for the pure corresponding crystalline TE, which shows that the local atomic structure in glassy alloys is different from that in hcp TE [2,5]. Indeed,  $N(E_F)$  and related magnetic and superconducting parameters of a-TEs agree quite well with those calculated for cubic phases of these metals [8] and are very different from those of hcp TEs. Simultaneously, such atomic structure results in reduced strength of interatomic bonding which shows up in low elastic moduli and Debye temperatures of a-TEs and TE-rich TE–TL glassy alloys (Fig. 3).

The relatively simple electronic structure of TE–TL metallic glasses [2] results in simple variations of several of their properties with composition. This enables one to predict the properties of, as-yet, unprepared amorphous alloys. Since many bulk metallic glasses (BMGs) are based on TE and TL components the systematic studies of binary TE–TL metallic glasses may be useful for the development of such BMGs.

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